# Mining Frequent User Query Patterns from XML Query Streams

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**Abstract:** An XML query stream is a massive and unbounded sequence of queries that are continuously generated at a fast speed from users over the Internet. Compared with traditional approaches of mining frequent user query patterns in static XML query databases, pattern mining in XML query streams is more challenging since several extra requirements need to be satisfied. In this paper, a mining algorithm is proposed to discover frequent user query patterns over an XML query stream. Unlike most of existing algorithms, the proposed algorithm works based on a novel encoding scheme. Through the scheme, only the leaf nodes of XML query trees are considered in the system and result in higher mining performance. The performance of the proposed algorithm is tested and analyzed through a series of experiments. These experiment results show that the XSM outperforms other algorithms in its execution time.

Keywords: Frequent XML query pattern, XML query stream mining, encoding scheme, database.

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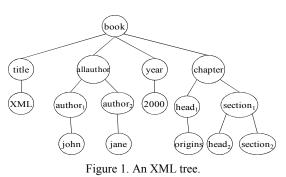
## 1. Introduction

XML query stream mining [1, 4, 11] has become a more and more attractive research area in recent years due to XML [8] has become the de facto standard language for information exchange over the Internet. An XML query stream is a massive and unbounded sequence of queries that are continuously generated from users to query XML data over the Internet. Due to this reason, as compared with traditional XML query pattern mining [5, 10, 12] in static databases, pattern mining in XML query streams has several requirements that need to be satisfied. For example, each user query in the XML query stream can be examined at most one time, that is, multiple scans of data source is infeasible.

An XML query stream [2, 3, 6, 13] comprises a continuous sequence of user queries which can be represented by multiple trees. Document data represented in XML comprise a sequence of possibly nested tags which can be expressed by a tree structure. Since XML data can be modeled as a tree, XML user queries are treated as trees. For example in Figures 1 and 2, they show an XML tree and its corresponding XML query tree. As an example of the XML tree depicted in Figure 1, an XML element enclosed within a pair of an opening tag and a closing tag is denoted by its tag name with a suffix number for distinguishing itself from other elements with the same tag name. Therefore, XML user queries (i. e., XPath [9]) typically specify patterns of selection predicates on multiple elements specified that have some tree-structured relationships. The primitive tree-structured relationships are parent-child and ancestor-descendant.

For example in Figure 2, it shows a query tree which is modeled by the XPath expression: Book [title = 'XML']/ allauthor/ author [.='john']. This expression matches author elements that: Have the string value "john"., are descendants of book elements that have a child title element whose value is "XML".

Mining frequent XML user query patterns may be used to enhance the query performance of XML streams. Frequent XML query patterns can be used to design an index mechanism or cache the results of these patterns to reduce the unnecessary computation and thus enhance the query performance. Using frequent XML query patterns, the features (i. e., contents and structures) of query results (i. e., the fragments of XML data in steams) are discovered and thus a suitable index mechanism can be designed. On the other hand, frequent XML query patterns can be used to support for storing a collection of XML data's fragments which are the answers of XML query patterns into a cache.



Several methods [1, 4, 11] have been proposed for mining frequent user query patterns over an XML query stream. XQSMinerI is a one pass algorithm to find out frequent user query patterns from XML query streams. XQSMinerII provides some control over the error bound in the estimate. XQSMinerI treats the stream of XML query trees as a stream of batches. This is because it is very expensive to enumerate frequent query patterns for all of query trees in a stream. In addition, XQSMinerII adopts the framework [6] and operates with two parameters, support  $\sigma$  and error  $\varepsilon$ , and processes the XML query stream in batch. The incoming stream is conceptually divided into buckets and in every batch it processes a number of buckets of query trees, where the number of buckets is dependent on the size of buffer. The local mining result of every batch is integrated into a data structure DTS which is a set of entries of potential frequent query patterns.

In this paper, an efficient algorithm (namely XSM) is proposed to mine frequent query patterns from XML query streams. XSM utilizes the framework [6] for approximate frequency count of query patterns. In XSM, an encoding scheme (namely XSCode) to represent an XML tree with its corresponding user query trees is proposed. XSCode is more space-efficient since it preserves the structure information of an XML query tree by only recording the codes of its leaf nodes. Through these codes, the frequent query stream in XSM.

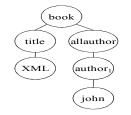


Figure 2. An XML query tree.

The rest of this paper is organized as follows: Section 2 illustrates a tree model of XML data. Section 3 describes the details of XSM. Section 4 shows the experimental results, and section 5 illustrates the conclusion and further work.

## 2. Preliminaries

- Definition 1: An XML query can be modeled as an unordered tree T =<N, E>, where N is the node set, and E is the edge set. Nodes n∈N represent the elements, attributes, and string values in an XML query, and edges e ∈ E represents the parent-child relationships denoted by "/".
- *Definition 2*: Given an XML query tree  $T = \langle N, E \rangle$  and an XML query rooted subtree  $t_i = \langle N_i, E_i \rangle$ .  $t_i$  is considered to be the *i*<sup>th</sup> rooted subtree of *T* iff there exists:

$$Root(t_i) = Root(T)$$
 (1)

Where  $Root(t_i)$  and Root(T) are the functions which return the root nodes of  $t_i$  and T respectively.

$$N_i \subseteq N, E_i \subseteq E \tag{2}$$

- Definition 3: An XML query stream,  $XQS = \langle T_1, T_2, ..., T_n \rangle$ , where *n* is the length of current stream, that is, the number of query trees seen so far.
- Definition 4: Given an XML query stream XQS, a minimum support value  $\sigma$  ranging from (0, 1], and an error parameter  $\varepsilon$  ranging from (0, 1], construct an algorithm to produce a set of frequent XML query trees  $t_i$  f along with their estimated frequencies on request. For any XML query tree  $t_i$ , let  $count_{true}(t_i)$  denote the true frequency of  $t_i$ , and  $count(t_i)$  denote the estimated frequency of  $t_i$ . The  $t_i$  produced has the following guarantees:
  - 1. For any  $t_i$  in the current stream, if  $count_{true}(t_i) \ge \sigma \times n$ , then we have  $t_i \in f$ .
  - 2. For any  $t_i$  that is considered to be frequent, we have  $count_{true}(t_i) \ge (\sigma \varepsilon) \times n$ .
  - 3. For any  $t_i$ , its estimated frequency  $count(t_i) \ge count_{true}(t_i) \varepsilon \times n$ .

Definition 1 defines an XML query as a tree. Definition 2 defines an XML query rooted subtree. Definition 3 illustrates an XML query stream *XQS* which contains multiple XML query trees. Each query tree in *XQS* represents a transaction associated with its transaction *ID*. For example in Figure 3, the XML query stream  $XQS = \langle T_1, T_2, ..., T_{100}, T_{101}, T_{102}, T_{103}, T_{104}, T_{105}, ..., T_{200} \rangle$ , where  $T_1, T_2, ..., T_{100}, T_{101}, T_{102}, T_{103}, T_{104}, T_{105}, ..., T_{200}$  are the user query trees and with their transaction *ID*s 1, 2, ..., 100, 101, 102, ..., 200 respectively. Also, the length of *XQS* is equal to 200.

## 3. Mining Frequent Query Pattern Over XML Query Streams

#### 3.1. XSCode

XSCode encodes the nodes of an XML tree in an xy coordinate system where xy are the coordinates of the two-dimensional space. The following symbols T, r, k, p, l, fc, and nc are used to represent the nodes in an XML tree. Symbol T represents an XML tree, r indicates the root node in T, k represents a node in T, p indicates the parent node of k, l represents the left sibling node of k, fc denotes the first child node of k, and nc represent the child node of k expect the first child fc. The encoding rules are described for the nodes in an XML tree T and listed as follows:

- 1. For an XML tree *T*, the root node *r* is set on the origin whose coordinates *x* and *y* are (0, 0).
- 2. For any node k in the tree T, if k is the fc node of its parent node p and p's coordinates are  $(x_p, y_p)$ , then k's coordinates are  $(x_p + 1, y_p + 1)$ .
- 3. For any node k in the tree T, if k is the nc node of its parent node p and its left sibling node l has m descendant nodes with the coordinates  $(x_l, y_l)$ . If m = 0 then k's coordinates are  $(x_l + 1, y_l)$ , otherwise, k's coordinates are  $(x_l + m, y_l)$ .

Note that, hereafter; the coordinates of an XML node

based on XSCode are namely *xscode*.

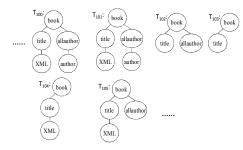


Figure 3. The XML query stream XQS.

• *Example 1*: Consider the XML tree in Figure 1. Suppose that all of nodes in the tree are encoded by the rules of XSCode. The *xscodes* of these nodes are shown in Figure 4. According to Rule 1, the root node *book* in the XML tree in Figure 1 is set on the origin and its *xscode* is (0, 0). According to Rule 2, the nodes *title*, *XML*, *author*<sub>1</sub>, *john*, *jane*, *2000*, *head*<sub>1</sub>, *origins*, and *head*<sub>2</sub> are the *fc* nodes of a node in the tree and their *xscodes* are (1, 1), (2, 2), (3, 2), (5, 3), (4, 3), (5, 2), (6, 2), (7, 3), and (8, 3) respectively. Also, by Rule (3), the nodes *allauthor*, *year*, *chapter*, *author*<sub>2</sub>, *section*<sub>1</sub>, and *section*<sub>2</sub> are the *nc* nodes of a node in the tree and their *xscodes* are (2, 1), (4, 1), (5, 1), (4, 2), (7, 2), and (9, 3) respectively.

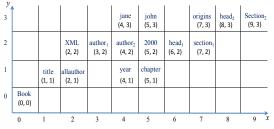


Figure 4. The xscodes of the nodes in Figure 1.

Derived from the XSCode encoding rules, Lemmas 1 and 2 show the features of *xscodes* of an XML tree.

- Lemma 1: For any node *f* in an XML tree *T<sub>i</sub>*, if *f*'s *xscode* is (*x*, *y*), then the value of *y* is equal to the level *l* of the node *f* in *T<sub>i</sub>*.
- *Proof*: We prove the lemma by showing that the value of *y* is equal to that of *l*. There are three cases, depending on whether node *f* is the root, *fc*, or *nc* node in *T<sub>i</sub>*.
- *Case 1*: Suppose that node *f* is the root node in *T<sub>i</sub>*. According to Rule 1, the *xscode* of *f* is (0, 0). Thus, the value of *y* is equal to 0. Also, since *f* is the root node, *f*'s level *l* is equal to 0. As a result, the value of *y* is equal to that of *l*.
- *Case 2*: Suppose that *f* is the *fc* node in *T<sub>i</sub>*. Since *f* is not the root node and with the level *l*, it has the ancestor nodes *p<sub>0</sub>*, *p<sub>1</sub>*,.., *p<sub>l-1</sub>*, where *p<sub>l-1</sub>* is *f*'s parent node, *p<sub>l-2</sub>* is *p<sub>l-1</sub>*'s parent node,..., and *p<sub>0</sub>* is the root node. According to Rule 1, the *xscode* of *p<sub>0</sub>* is (0, 0). Thus, *y<sub>p0</sub>* is equal to 0. Also, according to Lemma 2,

 $p_l$ 's xscode  $y_{pl} = y_{p0} + 1$ . Thus,  $y_{pl} = y_{p0} + 1 = 0 + 1$ = 1. In consequence,  $p_2$ 's xscode  $y_{p2} = y_{pl} + 1 = 1 + 1 = 2$ . Therefore,  $p_{l-l}$ 's xscode  $y_{pl-l} = l - 1$ . Since *f* is the child node of  $y_{p-l}$ , *f*'s xscode  $y = y_{pl-l} + 1 = l - 1 + 1 = l$ . As a result, the value of *y* is equal to that of *f*'s level *l*.

• *Case 3*: Suppose that *f* is the *nc* node and thus has a sibling node *fc* in  $T_i$ . According to Case 2, the *fc*'s *xscode*  $y_{fc} = l$ . In consequence, according to Rule 3, *f*'s *xscode y* is equal to  $y_{fc}$ . As a result,  $y = y_{fc} = l$  and the value of *y* is equal to that of *f*'s level *l*.

Based on Case 1, Case2, and Case 3, we thus prove this lemma.

- Lemma 2: For any two nodes  $f_1$  and  $f_2$  in an XML tree  $T_i$  with the *xscodes*  $(x_1, y_1)$  and  $(x_2, y_2)$  respectively, if node  $f_2$  is a descendant node of  $f_1$ , then both of the values of  $x_2$  and  $y_2$  are bigger than those of  $x_1$  and  $y_1$  respectively.
- *Proof*: We prove the lemma by showing that  $x_2 > x_1$  and  $y_2 > y_1$ . There are two cases, depending on whether node  $f_2$  is a child node or not of  $f_1$ .
- *Case 1*: Suppose that node  $f_2$  is a child node of  $f_1$ . If  $f_2$  is the first child node of  $f_1$ , according to Rule 2, the *xscode*  $(x_2, y_2)$  of  $f_2$  is equal to  $(x_1 + 1, y_1 + 1)$ ; otherwise, that is equal to  $(x_s + m, y_s)$ , where  $(x_s, y_s)$  is the *xscode* of  $f_1$ 's first child node  $f_s$  and  $f_s$  has m descendant nodes. Thus, if  $f_2$  is the first child node of  $f_1, x_2 = x_1 + 1$  and  $y_2 = y_1 + 1$  which result in  $x_2 > x_1$  and  $y_2 > y_1$  respectively. In addition, since  $x_2 = x_s + m$ ,  $y_2 = y_s, x_s = x_1 + 1$ , and  $y_s = y_1 + 1$  which result in  $x_2 > x_1$  and  $y_2 > y_s > y_1$ . As a result,  $x_2 > x_1$  and  $y_2 > y_1$ .
- *Case 2*: Suppose that node  $f_2$  is not a child node of  $f_1$  and has a parent node  $f_a$  which is a child node of  $f_1$ . According to Case 1, node  $f_a$ 's *xscode*  $x_{fa} > x_{f1}$  and  $y_{fa} > y_{f1}$ . Also, since  $f_2$ 's *xscode*  $x_{f2} > x_{fa}$  and  $y_{f2} > y_{fa}$ , they result  $x_{f2} > x_{f1}$  and  $y_{f2} > y_{f1}$ .

Based on Case 1 and Case2, we thus prove this lemma.

## 3.2. Functions X-Path and X-Subtree

In algorithm XSM, the path and subtree information of query trees in XML query streams are firstly considered by functions X-Path and X-Subtree. Symbols T,  $l_i$ , w,  $\varepsilon$ ,  $\beta$ ,  $B_{current}$ ,  $t_i$ ,  $a_i$ , count<sub>i</sub>, error<sub>i</sub>, sibling<sub>ij</sub>, s-count<sub>ij</sub>, and  $d_i$  are used in X-Path and X-Subtree. Symbol T represents an XML query tree,  $l_i$ indicates a leaf node of T,  $t_i$  represents the nodes which are stored in the system,  $a_i$  indicates an ancestor node of  $t_i$ , count<sub>i</sub> indicates the frequencies of  $t_i$ , error<sub>i</sub> shows  $t_i$ 's frequencies which are not recorded in the system, sibling<sub>ij</sub> indicates the sibling relationship between nodes  $t_i$  and  $t_j$ , *s*-count<sub>ij</sub> shows the frequencies of the sibling relationship between  $t_i$  and  $t_i$ , and  $d_i$  shows a descendant node of  $t_i$ . On the other hand, symbol  $\varepsilon$ denotes an error parameter. The incoming XML query stream is conceptually divided into buckets of  $w = \left[\frac{1}{\epsilon}\right]$ 

query trees. The buckets are labeled with bucket IDs starting from 1. The current bucket ID is denoted as  $B_{current}$ , whose value is  $\left\lceil \frac{n}{w} \right\rceil$ . Also, the number of

buckets in the main memory for the XML query stream is denoted as  $\beta$ . In function X-Path, the leaf nodes of XML query trees are concerned to record the path information of an XML query tree. If no node stored in the system, the leaf nodes of an XML user query tree are stored; otherwise, their *xscodes* are compared with those of nodes  $t_i$ . In addition, if *count*<sub>i</sub> >  $\beta$  and  $B_{current}$  >  $\beta$  in the system, the value of ( $B_{current} - \beta$ ) are set into their variables *error*<sub>i</sub>. In function X-Subtree, the relationship of a pair of leaf nodes of XML query trees is considered to deal with the subtree information of an XML query tree.

• *Example 2*: Suppose that all of the query trees  $T_1$ ,  $T_2$ , ..., and  $T_{200}$  in an XML query stream in Figure 3 are sequential read and processed by function X-Path. Also, suppose that query trees  $T_1, T_2, ..., T_{99}$  have been processed by X-Path and result in the stored nodes  $t_i$  as shown in Figure 5. Suppose that the error parameter  $\varepsilon$  is equal to 0.1 and the batch size is equal to 100. Therefore, a bucket has 10  $(1/\varepsilon=1/0.1)$  query trees,  $\beta$  is equal to 10  $(\left\lceil \frac{100}{10} \right\rceil = 10)$ ,

and  $B_{current}$  is equal to 10 ( $\left\lceil \frac{99}{10} \right\rceil = 10$ ). Firstly,  $T_{100}$  is

read and Lines 7-11 are executed since the leaf node *XML* of  $T_{100}$  is the same as the node  $t_1$ . Therefore, the value 1 is added into the variables *count*<sub>1</sub> and *count*<sub>3</sub> of  $t_1$  and  $t_3$  respectively. Also, Lines 27-28 are executed and the new node  $t_5$  is inserted between  $t_4$  and  $t_2$  since the leaf node *author* is a parent of  $t_2$ . Then,  $T_{101}$  is read and the value of  $B_{current}$  is changed to 11 (i. e.,  $\left\lceil \frac{101}{10} \right\rceil = 11$ ). Therefore, Lines 8-9 are

executed since the values of variables *conut*<sub>1</sub> and count<sub>5</sub> of  $t_1$  and  $t_5$  (i. e., values 26 and 86 respectively) are bigger than that of  $\beta$  (i. e., the value 10) and the value of  $B_{current}$  (i. e., the value 11) is bigger than that of  $\beta$ . As a result, the variables error<sub>1</sub>, error<sub>3</sub>, error<sub>4</sub>, and error<sub>5</sub> of  $t_1$ ,  $t_3$ ,  $t_4$ , and  $t_5$ respectively are set to value 1 (i.e.,  $B_{current} - \beta = 11$ -10). In consequence,  $T_{102}$  is read and Lines 20-24 are executed since the leaf nodes *title* and *allauthor* of  $T_{102}$  are the same as the nodes  $t_3$  and  $t_4$ respectively. Therefore, the value 1 is set into the variables *error*<sub>3</sub> and *error*<sub>4</sub> of  $t_3$  and  $t_4$  respectively. Then,  $T_{103}$  is read and Lines 21-25 are executed since  $T_{103}$ 's leaf node *title* is the ancestor of node  $t_1$ . Thus, the value of variable *error*<sub>3</sub> of  $t_3$  is set by the value 1.

Function X-Path (T,  $\varepsilon$ , size) Input: An XML query tree TOutput: nodes  $t_i$ 1 if there is no node stored in the system

2 store the nodes $l_i$ as $t_i$ and set variables $count_i$ with $l$ 3 else 4 for each leaf node $l_i$ of T 5 compare the $l_i$ 's xscode with that of each $t_i$ 6 if $l_i$ 's xscode is the same with that of $t_i$ then 7 if $((t_i's count_i) \ge \beta)$ and $(B_{current} > \beta)$ then 8 $t_i$ 's error <sub>i</sub> = $B_{current} - \beta$ 9 all of $t_i$ 's ancestor nodes $a_i$ 's error <sub>i</sub> = $B_{current} - \beta$ 10 else 11 add 1 to count <sub>i</sub> of $t_i$ and all of ancestor nodes $a_i$ 12 else 13 if $l_i$ is $t_i$ 's ancestor and their xscodes do not 14 stratify Lemma 2, and $t_i$ has no ancestor $a_i$ 15 store the node $l_i$ as a parent node $p_i$ of $t_i$ 16 set the value of count <sub>i</sub> of $p_i$ is the sum of that of 17 $t_i$ with value 1 18 if $((p_i's count_i) \ge \beta)$ and $(B_{current} > \beta)$ then 19 $p_i$ 's error <sub>i</sub> = $B_{current} - \beta$ 20 all of $p_i$ 's ancestor nodes $a_i$ 's error <sub>i</sub> = $B_{current} - \beta$ 21 if $l_i$ is an ancestor node of $t_i$ and $t_i$ has an 22 ancestor node $a_i$ which is the same as $l_i$ 23 if $((t_i's count_i) \ge \beta)$ and $(B_{current} > \beta)$ then 24 $t_i$ 's error <sub>i</sub> = $B_{current} - \beta$ 25 all of $t_i$ 's ancestor nodes $a_i$ 's error <sub>i</sub> = $B_{current} - \beta$ 26 else 27 add value 1 to count <sub>i</sub> of $a_i$ and all of $a_i$ 's 28 ancestor nodes 29 if $l_i$ is an ancestor node of $t_i$ and all of $a_i$ 's 21 ancestor nodes $a_i$ are different from $l_i$ 23 find $a_i$ which is a child node of $l_i$ 34 store node $l_i$ as a parent node $p_i$ of $a_i$ 's parent 35 set node $l_i$ as a parent node $p_i$ of $a_i$ 's parent 36 alse 37 if $l_i$ is a descendant node of $t_i$ 34 store node $l_i$ into a new created node $c_i$ 35 set node $l_i$ as a child node of $t_i$ 36 and 1 to count <sub>i</sub> and all of $c_i$ 's ancestors 37 if $l_i$ and $t_i$ have no ancestor-descendant 38 relationship 39 store $l_i$ into a new created node in system 40 end if 41 end for		
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<ul> <li>store l<sub>i</sub> into a new created node in system</li> <li>end if</li> <li>end for</li> </ul>		
40 end if 41 end for		1
41 end for		
0		0
42 enall	42	end if

43 return nodes  $t_i$ 

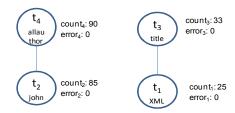


Figure 5. The nodes  $t_i$  after processing  $T_1$ ,  $T_2$ ,...,  $T_{99}$  in Figure 3 by X-Path.

After reading  $T_{104}$ , Lines 7-11 are executed and the values of variables *error*<sub>1</sub> and *error*<sub>3</sub> of  $t_1$  and  $t_3$  respectively are added by value 1 since the leaf node *XML* of  $T_{104}$  is the same as  $t_1$ . Finally,  $T_{105}$  is read and Lines 7-8 and 21-25 are executed. The values of variables *error*<sub>1</sub>, *error*<sub>3</sub> and *error*<sub>4</sub> of  $t_1$ ,  $t_3$ , and  $t_4$  respectively are set by the value 1 and result in Figure 6.

Also, suppose that all of query trees  $T_1, T_2, ...,$  and  $T_{200}$  in Figure 3 are sequential read and processed by

function X-Subtree. Suppose that the stored nodes  $t_i$  is shown in Figure 6 before executing X-Subtree. Firstly,  $T_{100}$  is read and Lines 3-8 in function X-Subtree are executed since the relationship between the leaf nodes XML and *author* are not recorded in their corresponding nodes  $t_1$  and  $t_5$ . Thus, *sibling*<sub>15</sub> is created and the variable *s*-count<sub>15</sub> is set to value 1. Then,  $T_{101}$  is read and processed by Lines 3-8 and the variable *s*-count<sub>15</sub> between  $t_1$  and  $t_5$  is added by value 1 since it is the same as  $T_{100}$ . In consequence,  $T_{102}$  is read and Lines 7-8 are executed since  $T_2$ 's leaf nodes *title* and allauthor are the ancestors of nodes  $t_1$  and  $t_5$ respectively. Thus, *sibling*<sub>34</sub> between nodes  $t_3$  and  $t_4$  is created. Also, the value of variable s-count<sub>34</sub> is set by the sum of value 1 and the value of  $d_i$ 's *s*-count<sub>ii</sub>. This is shown in Figure 7. In addition,  $T_{103}$  and  $T_{104}$  is read and not to be processed since it has no a pair of leaf nodes. Finally,  $T_{105}$  is read and then Lines 7-8 are executed and results in Figure 8.

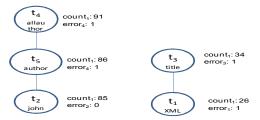


Figure 6. Nodes  $t_i$  for Figure 3 after executing X-Path.

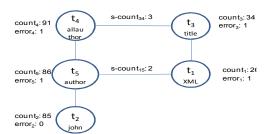


Figure 7. Nodes  $t_i$  for  $T_{100}$ ,  $T_{101}$ , and  $T_{102}$  in Figure 3 after executing X-Subtree.

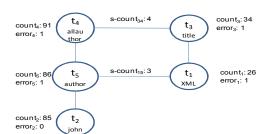


Figure 8. Nodes  $t_i$  for Figure 3 after executing X-Subtree.

Function X-Subtree(T) Input: An XML query tree T Output: nodes t<sub>i</sub>

- *l* for each pair of leaf nods  $l_i$  and  $l_i$  of T
- *2 if the sibling relationship between*  $l_i$  *and*  $l_j$  *is not*
- 3 stored
- 4 set the sibling<sub>ij</sub> relationships between  $t_i$  and  $t_j$
- 5 *if there is no variable s-count<sub>ij</sub> of the descendant*
- 6 nodes  $d_i$  of  $t_i$  and  $t_j$
- 7 set the variable s-count<sub>ij</sub> between  $t_i$  and  $t_j$  with 1

- 9 set the variable s-count<sub>ij</sub> between  $t_i$  and  $t_j$  with
- 10 the value which is the sum of the value of 11 variable s-count<sub>ii</sub> of  $d_i$  with  $d_i$  and value 1
- 12 else
- 13 add 1 to the s-count<sub>ii</sub> variables between  $t_i$  and  $t_i$
- 14 end if
- 15 end if
- 16 end for
- 17 return nodes  $t_i$

# 3.3. XSM

The following symbols  $t_i$ ,  $p_i$ ,  $(c_x, c_y)$ ,  $z_i$ ,  $temp\_x$ , ct, fp, and fs are used in algorithm XSM.  $t_i$  indicates the node which is stored in the system,  $p_i$  represents  $t_i$ 's parent node,  $(c_x, c_y)$  represents the *xscode* in  $t_i$ ,  $z_i$  indicates the sibling node of  $t_i$ , and *temp\_space* represents a temp space in the system. Symbol ctz indicates a subtree of nodes  $t_i$  and  $z_i$ . In addition, symbol fp indicates a set of frequent paths, while fs shows a set of frequent subtrees.

*Example 3*: Suppose that *XQS* has the query trees  $T_1$ ,  $T_2$ , ..., and  $T_{200}$  as shown in Figure 3 and a user issues an request when the query tree  $T_1$ ,  $T_2$ , ...,  $T_{105}$  have processed and sets  $\sigma = 0.3$ . Also suppose that the error parameter  $\varepsilon$  is equal to 0.1 and the batch size is equal to 100. Therefore, a bucket has 10 (1/ $\varepsilon$ =1/0.1) query trees,  $\beta$  is equal to 10 ( $\left\lceil \frac{100}{10} \right\rceil$ =10), and  $B_{current}$  is equal to

10 ( $\left\lceil \frac{99}{10} \right\rceil$  =10). Firstly, after executing Lines 3-5, the

information of the XML query stream is shown in Figure 8. Then, Figure 9 and 10 show the results after executing algorithm XSM. Figure 9 shows the results after executing Lines 5-12. In Figure 9, the values of *count<sub>i</sub>* of *t<sub>i</sub>* are bigger than 31.5 ( $\sigma * i = 0.3 * 105=31.5$ ). Finally, figure 10 presents sets *fp* and *fs* after executing Lines 14-25.

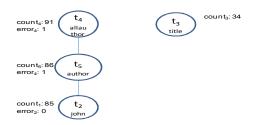


Figure 9. The frequent query patterns for Figure 3 after executing XSM.

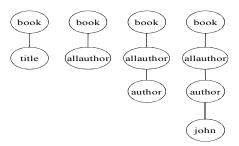


Figure 10. The frequent query patterns for Figure 3 after executing XSM.

8 else

Algorithm 1: XSM (XQS,  $\varepsilon$ , size,  $\sigma$ )

Input: The XML query stream XQS; The value of error parameter  $\varepsilon$ ; The size of batch size; Specified minimum support  $\sigma$ ; Output: A set of frequent query patterns from XQS

*1 Repeat* 

```
2 read a query tree T_i from XOS
```

- 3 X-Path $(T_i, \varepsilon, size);$
- 4 X-Subtree  $(T_i, \varepsilon, size);$
- 5 if  $(t_i \text{ 's count}_i + t_i \text{ 's error}_i)$  is small than  $B_{current}$
- $\begin{array}{c} 6 \\ 6 \\ \end{array} \begin{array}{c} delete \ the \ node \ t_i \end{array}$
- 7 *delete all of t<sub>i</sub>*'s ancestor nodes
- 8 end if
- *9 if a request issued from users*
- 10 copy all information into temp space
- 11 for each node  $t_i$  in temp\_space
- *12 if the value of count<sub>i</sub> is small than*  $\sigma * i$
- *13 delete the node*  $t_i$
- *l4 delete*  $t_i$ 's sibling nodes
- 15 delete all of  $t_i$ 's descendant nodes
- 16 end if
- 17 end for
- 18 /\* generate frequent subtrees from temp\_space; \*/
- 19 for each node  $t_i$  with xscode  $(c_x, c_y)$  in temp\_space
- 20 while  $c_x > 0$
- 21 add a path  $(p_i, t_i)$  into set fp
- *22 if*  $t_i$  has the sibling node  $z_i$
- *add the cross subtree ctz into set fs*
- 24 end if
- 25 set  $p_i$  is the parent of  $p_i$
- *26 end while*
- 27 delete  $t_i$
- 28 delete t<sub>i</sub>'s sibling nodes
- 29 end for
- 30 end if
- 31 Until not eof(XQS)

## 3.4. Comparison

One reason confirms that XSM may outperform XQSMinerI and XQSMinerII. XQSMinerI and XQSMinerII construct a Dynamic Transaction summary Structure (DTS) that summarizes the query patterns seen so far and keeps track of the transaction ID of each query pattern. Then, through tree-join process (i.e., constructing data structure *ECTree*), the single branch candidate subtrees are merged to produce the frequent query patterns. As a result, in XQSMinerI and XQSMinerII, more XML query trees are processed on DTS and thus cost a lot of time to produce frequent XML query patterns. In contrast, XSM encodes the path and subtree information in an XML query tree's leaf node and results in a few nodes are recorded to be tested. Therefore, the mining performance is enhanced.

## 4. Experimental Results and Analyses

In this section we are to appraise our algorithm XSM. Two experiments in total have been conducted to evaluate the performance of XSM. The two experiments were carried out on the platform of personal computer with P8 2.67 GHz dual core CPU and about 4 GB of available physical memory space. The operating system is Windows 7, and the programs of the algorithm are implemented in C++ (and complied by Dev-C++).

To simulate an XML query stream, we employ the XMARK.DTD [7] as the DTDs to generate the query trees. First of all, we translate the DTDs into DTD trees. Secondly, we generate a query tree database containing 90000 different queries. Finally, we randomly select a number of queries (ranging from 10000 to 90000) from the previous step to form an XML query stream. In consequence, in the two experiments, parameters and their settings are listed in Table 1. The parameter *n* denotes the number of XML query trees in an XML query stream. Parameter  $\varepsilon$  illustrates the maximum error in the system to mine the frequent user query patterns. Parameter  $\sigma$  represents the value of minimum support in the system, and the parameter *B* denotes the batch size in the system.

Table 1. Simulation parameters and settings.

Parameters	Descriptions	Settings
n	Number of XML query trees	20,000 ~ 90,000
3	Maximum error in the system	$0.008\sim 0.2$
σ	Minimum supports	1%~20%
В	Size of batch in the system	2,000 ~ 8,000

The first experiment, with results shown in Figure 11, observes the execution time (Y-axis) of XSM for different support levels under different batch size (X-axis). The specified maximum error  $\varepsilon$  is set to 0.1 in Figure 11. From Figure 11, we can infer that for XSM, the execution time taken decreases drastically as the batch size increases. The reduction in time taken is even more pronounced when the batch size is 3000. The reason is that for small batch sizes, the *xsnodes* in the system are deleted frequently in the system. In addition, using the higher support as the threshold to prune away infrequent query patterns results in higher performance and further reduces the execution time taken. As a result, it is important to choose an appropriate batch size for an XML query stream mining algorithm. The performance will deteriorate significantly if the batch size is too small.

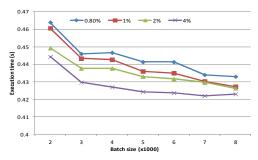


Figure 11. The execution time with varying batch size.

The second experiment, with results shown in Figure 12, observes the execution time (Y-axis) of XSM for different support levels under different maximum error (X-axis). The specified number of

queries in the batch B is set to 4,000 in Figure 12. From Figure 12, we can infer that for XSM, the execution time taken decreases drastically as the maximum error increases. The reduction in time taken is even more pronounced when the maximum error is 0.05. The reason is that, the number of query trees is deleted for high maximum error more than that for low maximum error and results in less query trees' information are preserved in the system.

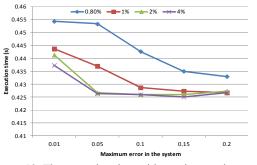


Figure 12. The execution time with varying maximum error.

# 5. Conclusions

In this paper, an efficient mining algorithm XSM is proposed to discover frequent XML query patterns from XML query streams. Unlike the existing algorithms, a new idea by encoding XML query trees (i. e., XSCode) is proposed and thus preserves the path and subtree information of query trees. With this idea, it became obvious that XSM is not capable of maintaining all of the user queries and thus takes less execution time and memory space to produce the frequent XML query patterns. Our future work includes expanding XML query patterns with repeating-siblings, since XSM cannot mine the frequent XML query patterns with sibling repetitions from an XML query stream.

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